試科目	統計学	系別	統計学系 34	考試時間	七月五日上午第 一 星期六

注意: 附常態分配表,卡方分配表,t 分配表,F 分配表於最後.

(36%) 1. In the following multiple choice questions, please give the correct answer. 每小題3分

1-1. A summary measure that is computed from a sample to describe a characteristic of the population is called

a. a parameter

b. a statistic

c. a population

d. Both a and c since they are the same

1-2. Which of the following is an example of nonsampling errors?

a. Errors that arise from the recording of incorrect responses.

b. Errors that arise when responses are not obtained from some members of the sample.

c. Errors that arise when some members of the target population cannot possibly be selected in the sample.

d. All of the above are examples of nonsampling errors.

1-3. Which of the following statements is correct given that the events A and B have nonzero probabilities?

a. A and B cannot be both independent and mutually exclusive

b. A and B can be both independent and mutually exclusive

c. A and B are always independent

d. A and B are always mutually exclusive

1-4. A larger standard deviation of a normal distribution indicates that the distribution becomes

a. narrower and more peaked

b. flatter and wider

c. more skewed to the right

d. more skewed to the left

1-5. Which of the following statements is false?

a. The width of a confidence interval estimate of the population mean narrows when the value of the sample mean increases

b. The width of a confidence interval estimate of the population mean narrows when the sample size increases

c. The width of a confidence interval estimate of the population mean widens when the confidence level increases

d. All of the above statements are true

1-6. A confidence interval is defined as:

a. a point estimate plus or minus a specific level of confidence

b. a lower and upper confidence limit associated with a specific level of confidence

c. an interval that has a 95% probability of containing the population parameter

d. a lower and upper confidence limit that has a 95% probability of containing the population parameter

1-7. If a hypothesis is not rejected at the 0.10 level of significance, it:
a. must be rejected at the 0.05 level
b. may be rejected at the 0.05 level
c. will not be rejected at the 0.05 level
d. must be rejected at the 0.025 level

1-8. Using the confidence interval when conducting a two-tail test for the population mean μ we do not reject the null hypothesis if the hypothesized value for μ:
a. is to the left of the lower confidence limit (LCL)
b. is to the right of the upper confidence limit (UCL)
c. falls between the LCL and UCL
d. falls in the rejection region

1-9. Which statistical technique is appropriate when we compare two populations of qualitative data with exactly two categories?
a. z-test of the difference between two proportions
b. The chi-squared test of a contingency table
c. The chi-squared test of goodness-of-fit
d. Both a and b
e. Both a and c

1-10. Given a specific value of x and confidence level, which of the following statements is correct?
a. The confidence interval estimate of the expected value of y can be calculated but the prediction interval of y for the given value of x cannot be calculated.
b. The confidence interval estimate of the expected value of y will be wider than the prediction interval.
c. The prediction interval of y for the given value of x can be calculated but the confidence interval estimate of the expected value of y cannot be calculated.
d. The confidence interval estimate of the expected value of y will be narrower than the prediction interval.

1-11. The adjusted multiple coefficient of determination is adjusted for the:
a. number of regression parameters including the y-intercept
b. number of dependent variables and the sample size
c. number of independent variables and the sample size
d. coefficient of correlation and the significance level

1-12. The problem of multicollinearity arises when the:
a. dependent variables are highly correlated with one another
b. independent variables are highly correlated with one another
c. independent variables are highly correlated with the dependent variable
d. both a and b are correct statement

(14%) 2. A random sample of 250 households in a large city revealed that the mean number of televisions per household was 2.70. From previous analyses we know that the population standard deviation is 1.8.

a. Can we conclude at the 5% significance level that the true mean number of televisions per household is not 2.5?

b. Refer to part (a), calculate the p-value.

c. Refer to part (a), compute the probability of a Type II error if the true mean number of televisions per household is 3.

(10%) 3. An industrial statistician wanted to determine if efforts to promote safety have been successful. By checking the records of 250 employees, she found that 33 of them suffered either minor or major injuries that year. A random sample of 400 employees last year revealed that 64 suffered some form of injury. Can the statistician conclude with $\alpha = 0.05$ that efforts to promote safety have been successful?

(15%) 4. A salesperson makes five calls per day. A sample of 200 days gives the frequencies of sales volumes listed below

Number of Sales	Observed Frequency (days)
0	10
1	38
2	69
3	63
4	18
5	2

Assume the population is binomial distribution with a probability of purchase p equal to 0.50. Should the assumption of a binomial distribution be rejected at the 5% significance level?

(25%) 5. A management consultant wants to compare the income of graduates of MBA programs with graduates of BBA programs. Assume that the two populations are normal with equal variances. In a random sample of 6 incomes five years after getting an MBA degree, the consultant found $\bar{x}_1 = \$45.3$ thousand and $s_1 = \$9.6$ thousand. A random sample of 8 incomes five years after getting a BBA degree yielded $\bar{x}_2 = \$43.6$ thousand and $s_2 = \$12.3$ thousand.

(a) Estimate the difference in mean incomes between MBA and BBA graduates. Use a confidence level of 99%.

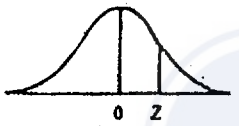
(b) Do these data present sufficient evidence to assume that a difference exists in mean incomes between MBA and BBA graduates? Use $\alpha = 0.05$.

(c) Can we use another test and draw the same conclusion as in part (b)? If your answer is 'yes', please show your work.

國立政治大學九十二 學年度轉學生入學考試

考試科目	統計学	系別	統計学系	考試時間	七月五日上午第二節 星期六

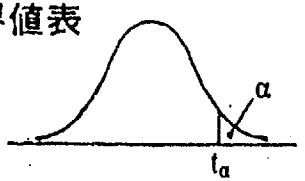
標準常態分配表



Example:
If $Z = 1.00$, then the area between the mean and this value of Z is .3413.

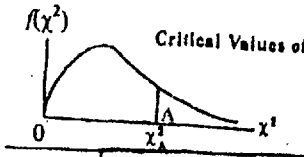
Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4777	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.49865	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
4.0	.49997									

t分配臨界值表



Degrees of Freedom	$t_{.100}$	$t_{.050}$	$t_{.025}$	$t_{.010}$	$t_{.005}$
1	3.078	6.314	12.706	31.821	63.657
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.747	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.753	2.131	2.602	2.947
16	1.337	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845
21	1.323	1.721	2.080	2.518	2.831
22	1.321	1.717	2.074	2.508	2.819
23	1.319	1.714	2.069	2.500	2.807
24	1.318	1.711	2.064	2.492	2.797
25	1.316	1.708	2.060	2.485	2.787
26	1.315	1.706	2.056	2.479	2.779
27	1.314	1.703	2.052	2.473	2.771
28	1.313	1.701	2.048	2.467	2.763
29	1.311	1.699	2.045	2.462	2.756
∞	1.282	1.645	1.960	2.326	2.576

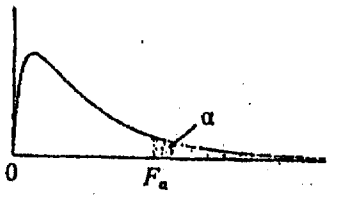
卡方分配臨界值表



DEGREES OF FREEDOM	$\chi^2_{.995}$	$\chi^2_{.990}$	$\chi^2_{.975}$	$\chi^2_{.950}$	$\chi^2_{.900}$	$\chi^2_{.100}$	$\chi^2_{.050}$	$\chi^2_{.025}$	$\chi^2_{.010}$	$\chi^2_{.005}$
1	0.0000393	0.0001571	0.0009821	0.0039321	0.0157908	2.70554	3.84146	5.02389	6.63490	7.87944
2	0.0100251	0.0201007	0.0506356	0.102587	0.210720	4.60517	5.99147	7.37776	9.21034	10.5966
3	0.0717212	0.114832	0.215795	0.351846	0.584375	6.25139	7.81473	9.34840	11.3449	12.8381
4	0.206990	0.297110	0.484419	0.710721	1.063623	7.77944	9.48773	11.1433	13.2767	14.8602
5	0.411740	0.554300	0.831211	1.145476	1.61031	9.23635	11.0705	12.8325	15.0863	16.7496
6	0.675727	0.872085	1.237347	1.63539	2.20413	10.6446	12.5916	14.4494	16.8119	18.5476
7	0.989265	1.239043	1.68987	2.16735	2.83311	12.0170	14.0671	16.0128	18.4753	20.2777
8	1.344419	1.646482	2.17973	2.73264	3.48954	13.3616	15.5073	17.5346	20.0902	21.9550
9	1.734926	2.087912	2.70039	3.32511	4.16816	14.6837	16.9190	19.0228	21.6660	23.5893
10	2.15585	2.55821	3.24697	3.94030	4.86518	15.9871	18.3070	20.4831	23.2093	25.1882
11	2.60321	3.05347	3.81575	4.57481	5.57779	17.2750	19.6751	21.9200	24.7250	26.7569
12	3.07382	3.57056	4.40379	5.22603	6.30380	18.5494	21.0261	23.3367	26.2170	28.2995
13	3.56503	4.10691	5.00874	5.89186	7.04150	19.8119	22.3621	24.7356	27.6883	29.8194
14	4.07468	4.66043	5.62872	6.57063	7.78953	21.0642	23.6848	26.1190	29.1413	31.3193
15	4.60094	5.22935	6.26214	7.26094	8.54675	22.3072	24.9958	27.4884	30.5779	32.8013
16	5.14224	5.81221	6.90766	7.96164	9.31223	23.5418	26.2962	28.8454	31.9999	34.2672
17	5.69724	6.40776	7.56418	8.67176	10.0852	24.7690	27.5871	30.1910	33.4087	35.7185
18	6.26481	7.01491	8.23075	9.39046	10.8649	25.9894	28.8693	31.5264	34.8053	37.1564
19	6.84398	7.63273	8.90655	10.1170	11.6509	27.2036	30.1435	32.8523	36.1908	38.5822
20	7.43386	8.26040	9.59083	10.8508	12.4426	28.4120	31.4104	34.1696	37.5662	39.9968
21	8.03366	8.89720	10.28293	11.5913	13.2396	29.6151	32.6705	35.4789	38.9321	41.4010
22	8.64272	9.54249	10.9823	12.3380	14.0415	30.8133	33.9244	36.7807	40.2894	42.7956
23	9.26042	10.19567	11.6885	13.0905	14.8479	32.0069	35.1725	38.0757	41.6384	44.1813
24	9.88623	10.8564	12.4011	13.8484	15.6587	33.1963	36.4151	39.3641	42.9798	45.5585
25	10.5197	11.5240	13.1197	14.6114	16.4734	34.3816	37.6525	40.6465	44.3141	46.9278
26	11.1603	12.1981	13.8439	15.3791	17.2919	35.5631	38.8852	41.9232	45.6417	48.2899
27	11.8076	12.8786	14.5733	16.1513	18.1138	36.7412	40.1133	43.1944	46.9630	49.6449
28	12.4613	13.5648	15.3079	16.9279	18.9392	37.9159	41.3372	44.4607	48.2782	50.9933
29	13.1211	14.2565	16.0471	17.7083	19.7677	39.0875	42.5569	45.7222	49.5879	52.3356
30	13.7867	14.9535	16.7908	18.4926	20.5992	40.2560	43.7729	46.9792	50.8922	53.6720
40	20.7065	22.1643	24.4331	26.5093	29.0505	51.8050	55.7585	59.3417	63.6907	66.7659
50	27.9907	29.7067	32.3574	34.7642	37.6886	63.1671	67.5048	71.4202	76.1539	79.4900
60	35.5346	37.4848	40.4817	43.1879	46.4589	74.3970	79.0819	83.2976	88.3794	91.9517
70	43.2752	45.4418	48.7576	51.7393	55.3290	85.5271	90.5312	95.0231	100.425	104.215
80	51.1720	53.5400	57.1532	60.3915	64.2778	96.5782	101.879	106.629	112.329	116.321
90	59.1963	61.7541	65.6466	69.1260	73.2912	107.565	113.145	118.136	124.116	128.299
100	67.3276	70.0648	74.2219	77.9295	82.3581	118.498	124.342	129.561	135.807	140.169

F 分配臨界值表

$P(F > F_\alpha) = \alpha$



	ν_1(d.f.)				$\alpha = 0.05$				
ν_2(d.f.)	1	2	3	4	5	6	7	8	9
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96
∞	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88

試科目	微積分	系別	統計系 34	考試時間	7月5日上午第 星期六下

) ① Find $\lim_{(x,y)\to(0,0)} \frac{\sin(4x^2+4y^2)}{x^2+y^2} = ?$

② Find $\lim_{x\to 0} \frac{\int_{2x}^{3x} e^{t^2+4}\,dt}{x\,e^{x^2}} = ?$

③ Does $\lim_{(x,y)\to(0,0)} \frac{xy^2}{x^2+y^4}$ exist ? why ?

2) Find ① $\int_0^{\frac{\pi^2}{4}} \cos\sqrt{x}\,dx = ?$

② $\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} (\cos x)^2 \cot x\,dx = ?$

③ $\int_0^1 x\tan^{-1}x\,dx = ?$

3) $\begin{cases} f(x) = x^4 \sin\frac{4}{x}, & x\neq 0 \\ f(0) = 0 \end{cases}$

Find $f'(0) = ?$ $f'(1) = ?$

) $z + \sin(3y+2x) = \cos(3x+y)$. Find $\frac{\partial z}{\partial x} = ?$

) ① Express the volume of the solid between $z = 4-x^2-y^2$ and $z = 1$ as an iterated integral $\int_?^? dx \int_?^? (\ ?\ )\,dy$. Do not integrate.

② Reverse the order of integration $\int_0^1 dy \int_y^{\sqrt[3]{y}} f(x,y)\,dx$.

) Find the absolute extrema of $f(x,y) = x^2+xy+y^2+4$, where $x^2+y^2 \le 8$.